



**KIAPS**

KOREA INSTITUTE OF  
ATMOSPHERIC PREDICTION SYSTEMS

# Impacts of Spatial Observation Error Correlation in AMVs on Data Assimilation

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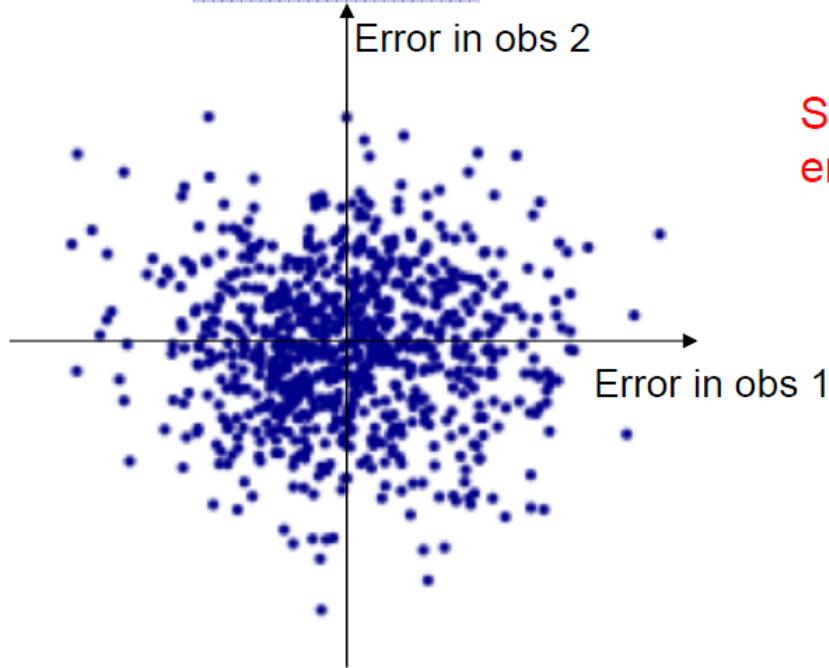
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# Error Correlation

$$J(\mathbf{x}) = \frac{1}{2}(\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1}(\mathbf{x} - \mathbf{x}_b) + \frac{1}{2}(\mathbf{y} - \mathbf{H}[\mathbf{x}])^T \mathbf{R}^{-1}(\mathbf{y} - \mathbf{H}[\mathbf{x}])$$

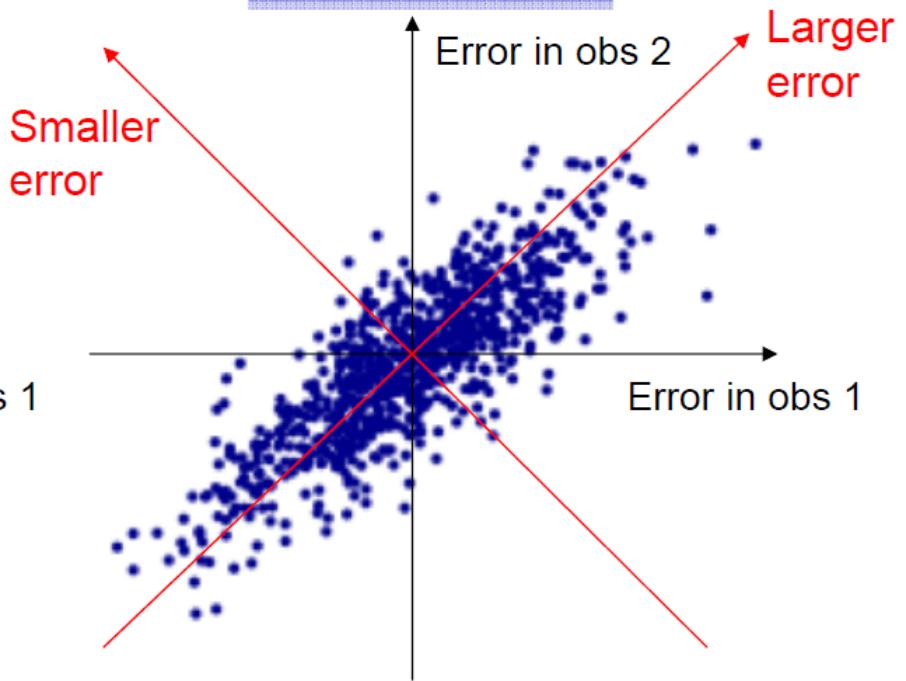
Uncorrelated error

$$\mathbf{R} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$



Correlated error

$$\mathbf{R} = \begin{pmatrix} 1 & 0.8 \\ 0.8 & 1 \end{pmatrix}$$



**Objective :** To characterize the spatial error correlation of COMS and MTSAT AMVs

**Method :**

**1. Pairs of collocations with sonde and AMVs :**

horizontal < 150 km, vertical < 25 hPa, vector difference < 18 m/s

**2. AMV-sonde departure correlation ( $R$ ) =  $0.5( \langle \Delta u, \Delta u \rangle + \langle \Delta v, \Delta v \rangle )$**

**3. Correlation function:**  $R(r) = R_0 ( 1 + r/L ) e^{-r/L}$

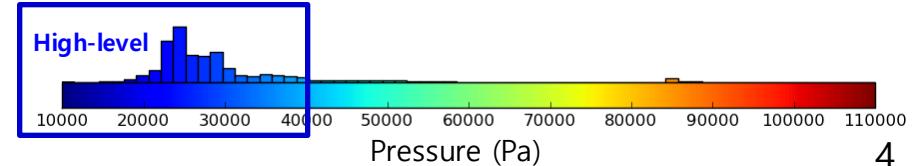
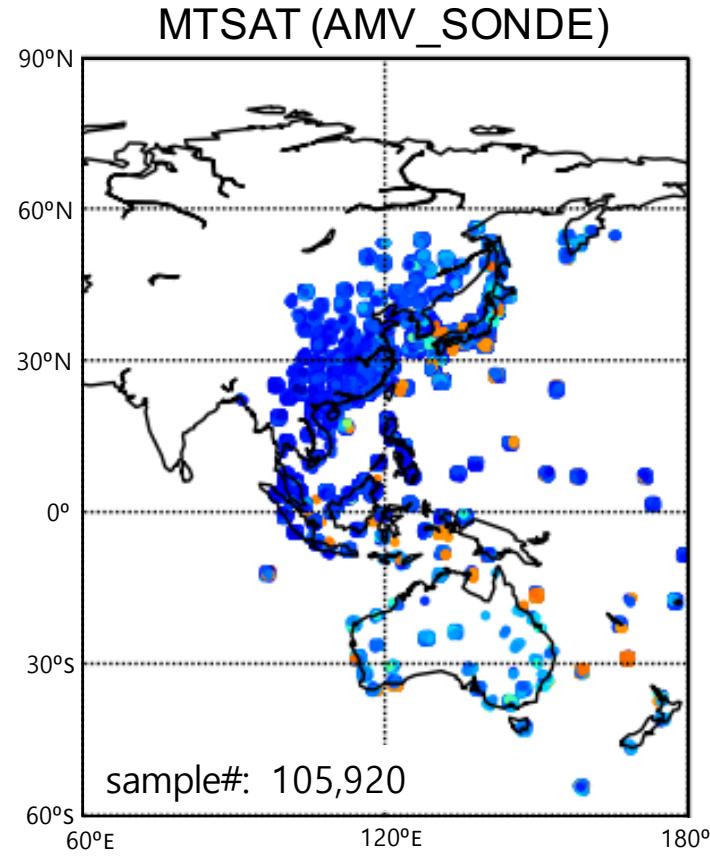
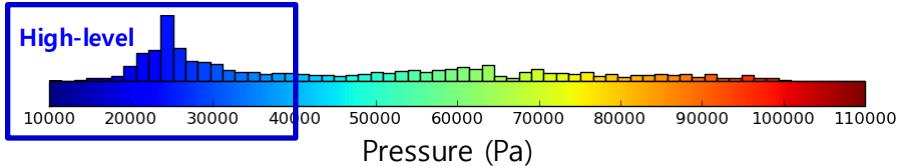
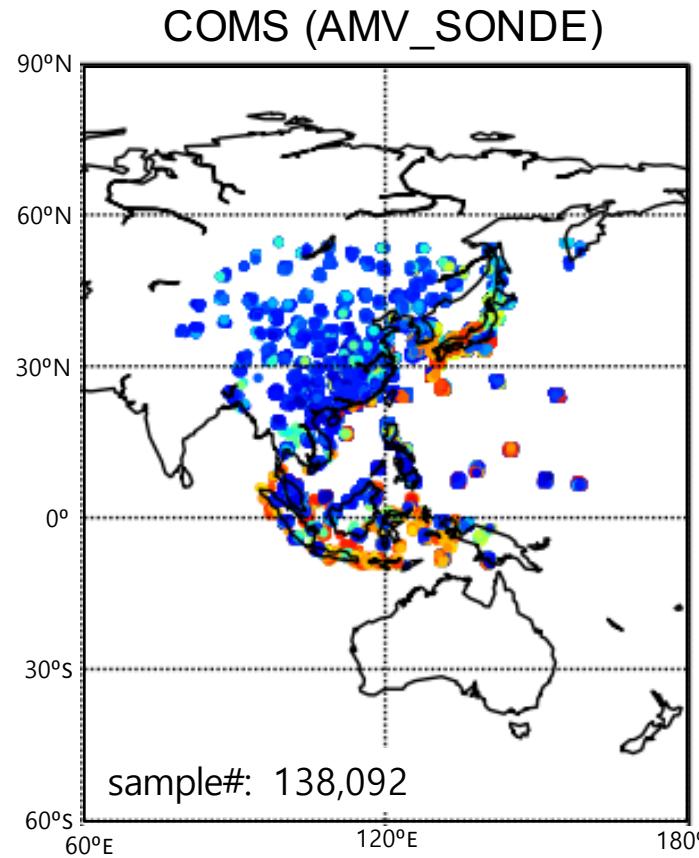
**4. Covariance matrix with spatial error correlation**

**5. Comparison of variances in eigen mode and observation space**

**6. Same steps with sonde and background**

# Collocated Sonde and AMVs

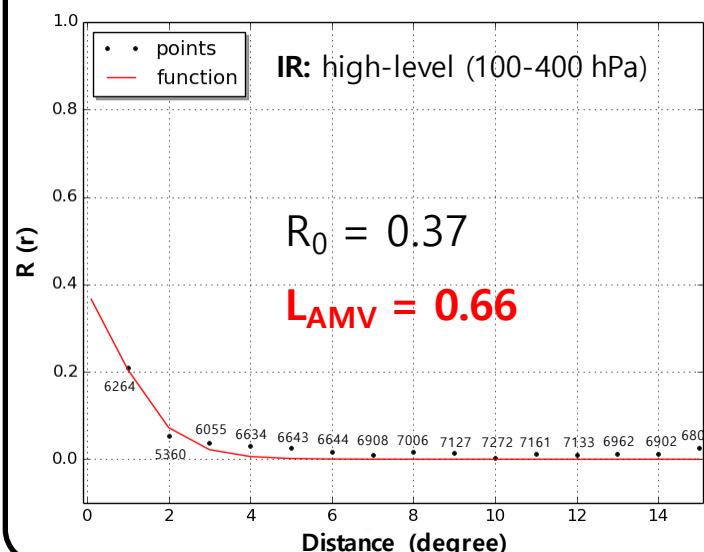
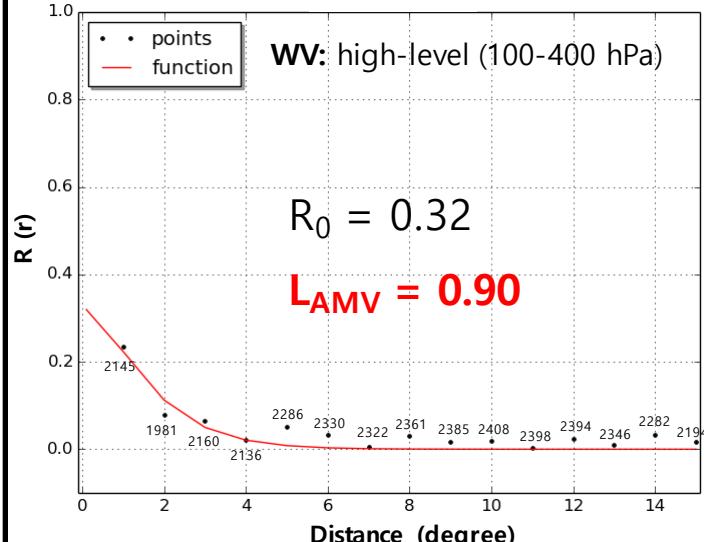
- Period: 2015070100-2015073118
- Sonde (w/ windprofiler), **COMS AMVs** (QI80\_fc: IR, WV & VIS), and **MTSAT AMVs** (QI80\_fc: IR & WV)



# AMV-Sonde

## COMS

AMV-Sonde

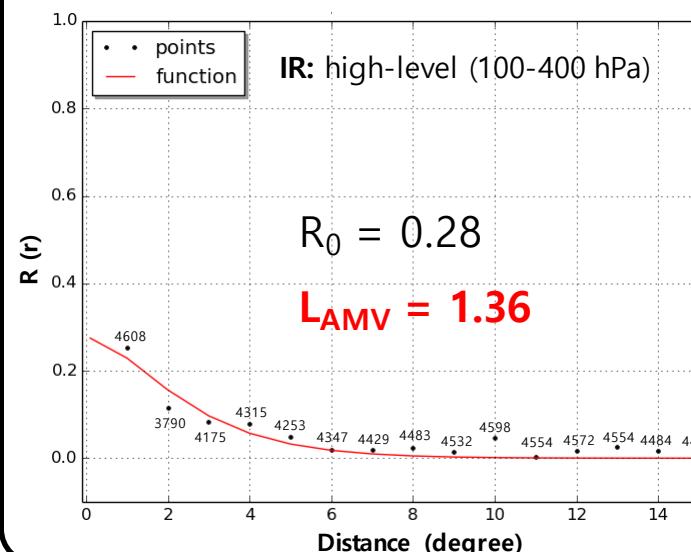
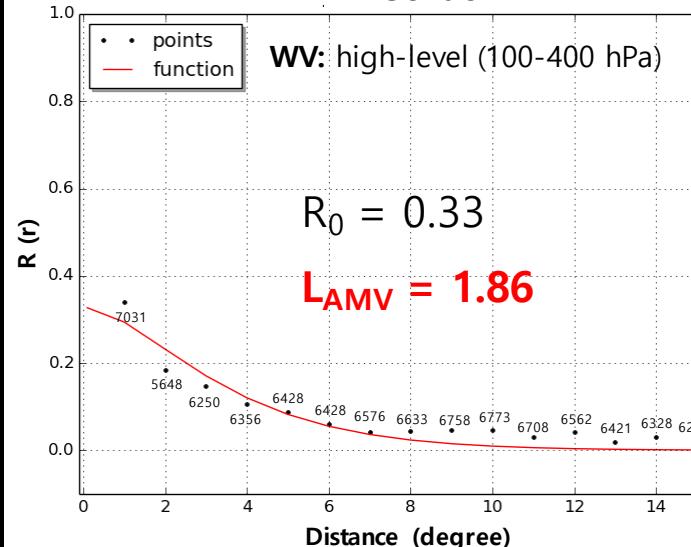


# Departure Correlation (I)

$$R(r) = R_0 (1 + r/L) e^{-r/L}$$

## MTSAT

AMV-Sonde



Assume sondes are spatially uncorrelated.

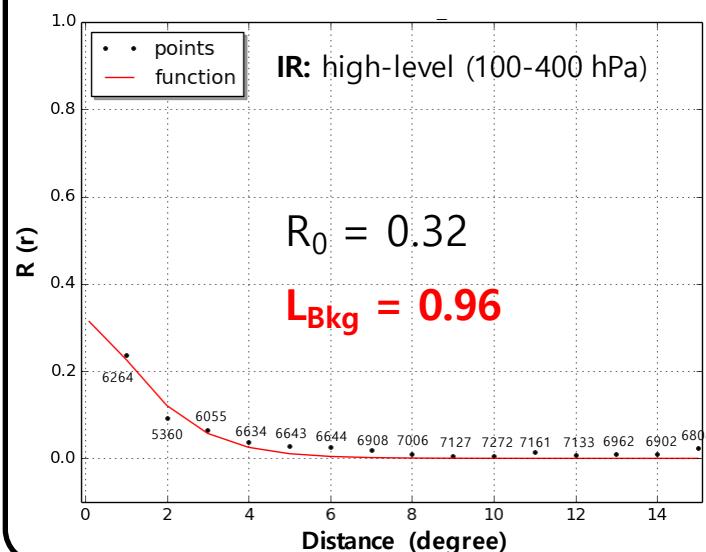
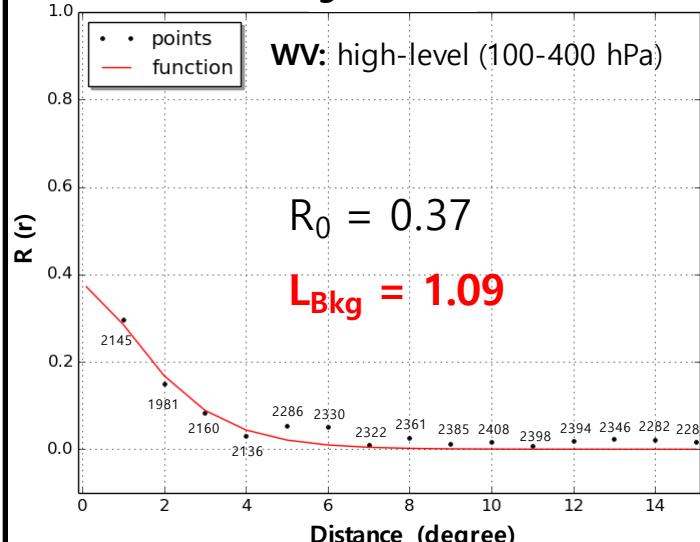
The correlation length scales ( $L$ ) of **MTSAT AMVs** are longer than those of COMS AMVs. This fitting parameter shows larger spatially correlated error in MTSAT AMVs.

In both satellites, the correlations of the AMV-sonde differences tend to be larger for **WV AMVs** compared to IR AMVs.

# Background-Sonde

## COMS

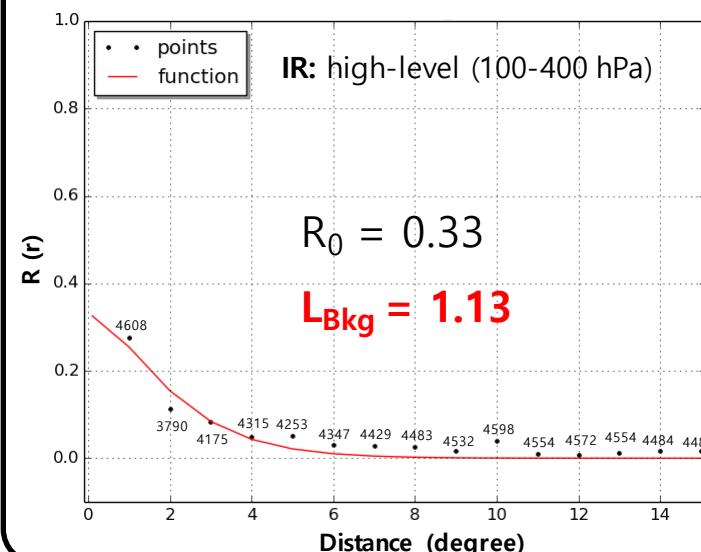
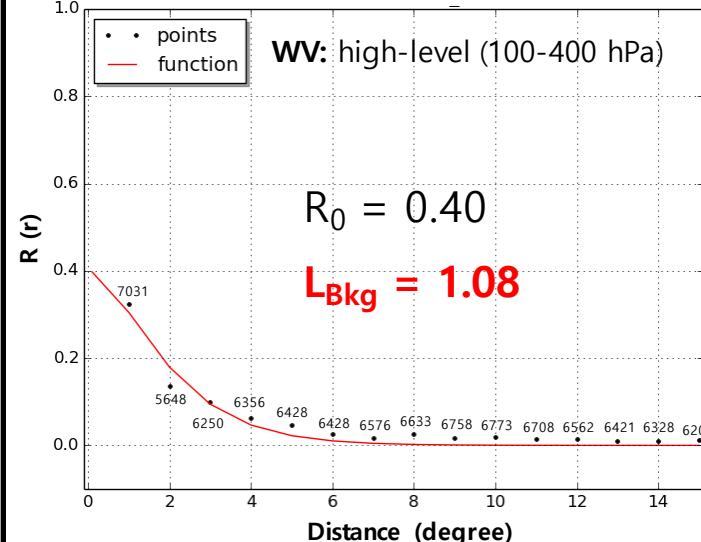
### Background-Sonde



# Departure Correlation (II)

## MTSAT

### Background-Sonde



$$R(r) = R_0 (1 + r/L) e^{-r/L}$$

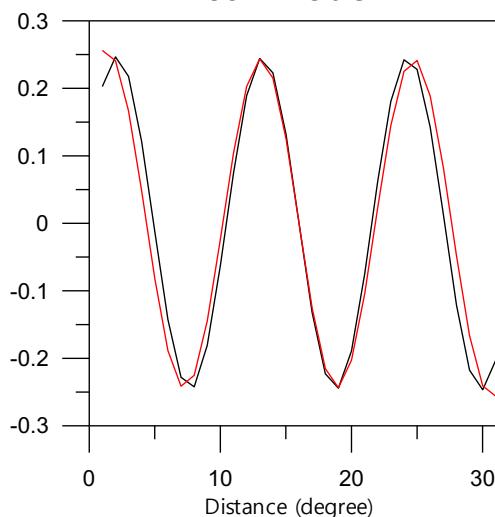
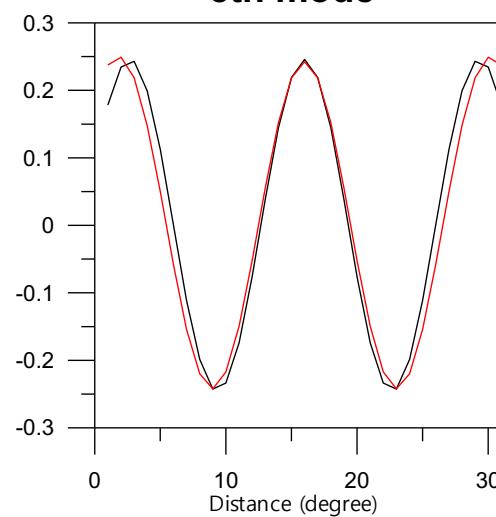
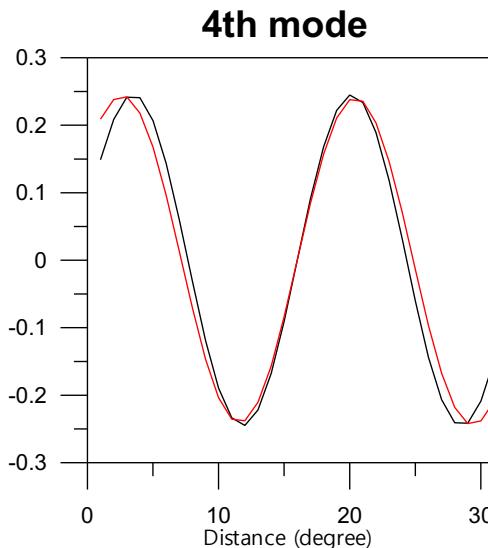
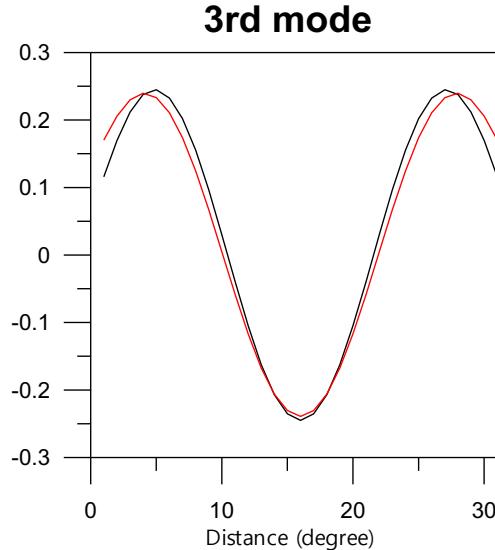
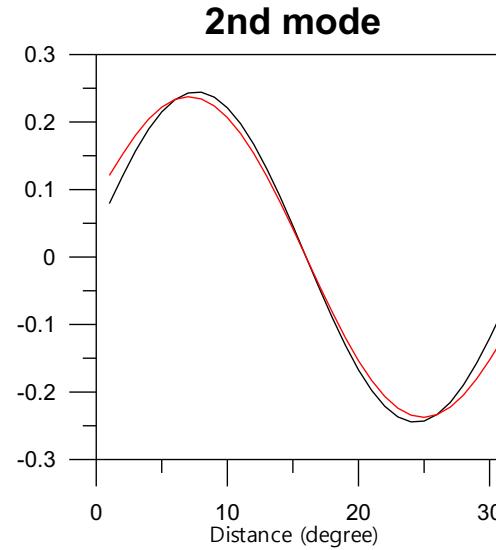
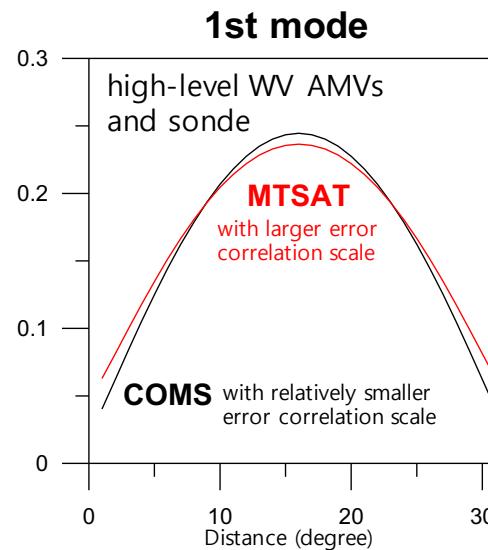
Assume sondes are spatially uncorrelated.

**Background:**  
KIAPS Integrated  
Model (KIM) v2.3

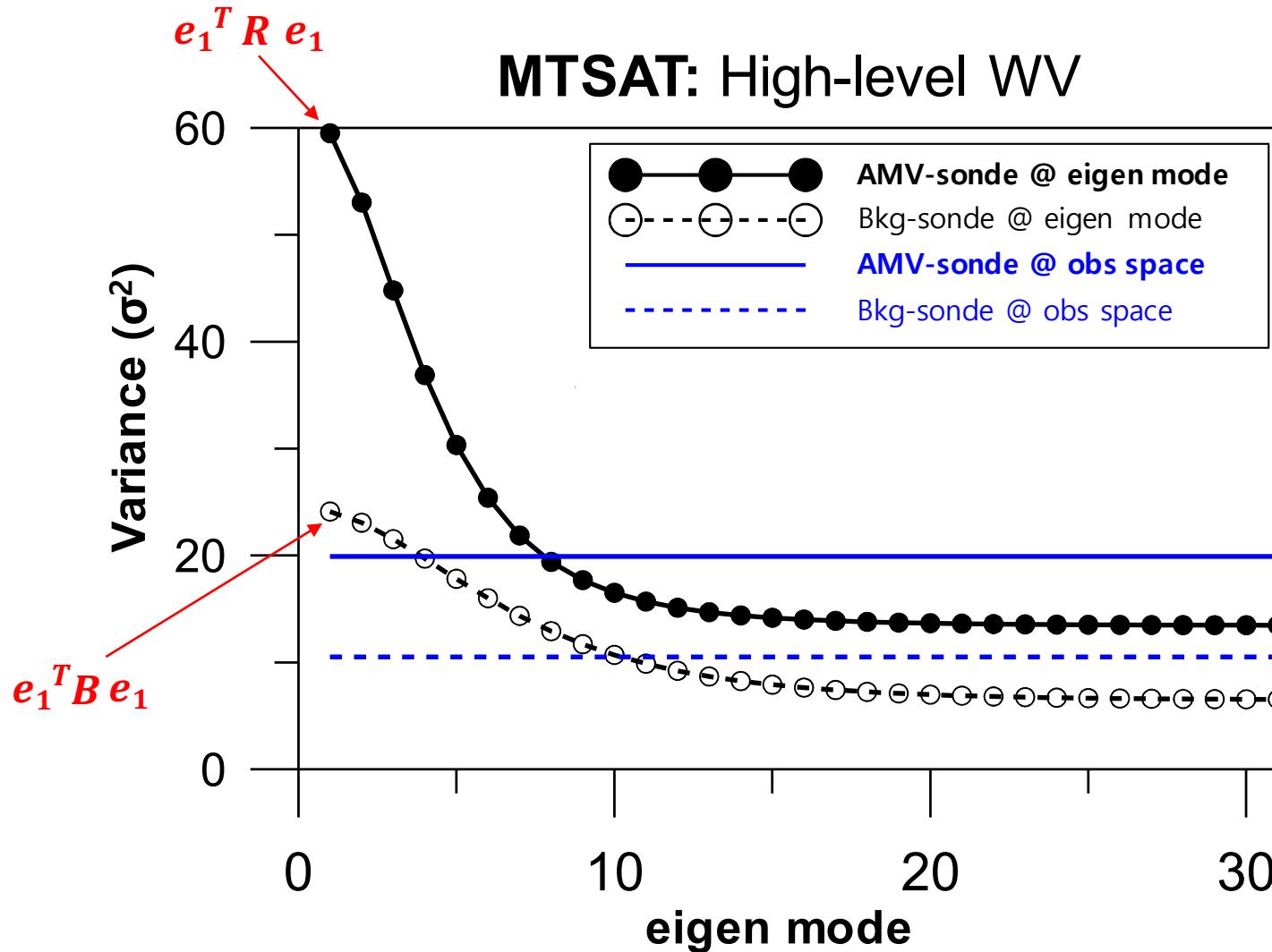
The background winds in collocated COMS and MTSAT AMVs give similar error correlations with length scale of 0.96 to 1.13.

- COMS:  $L_{AMV} < L_{Bkg}$
- MTSAT:  $L_{AMV} > L_{Bkg}$

## Eigenvectors of the error correlation matrix



# Spatial Error Correlation



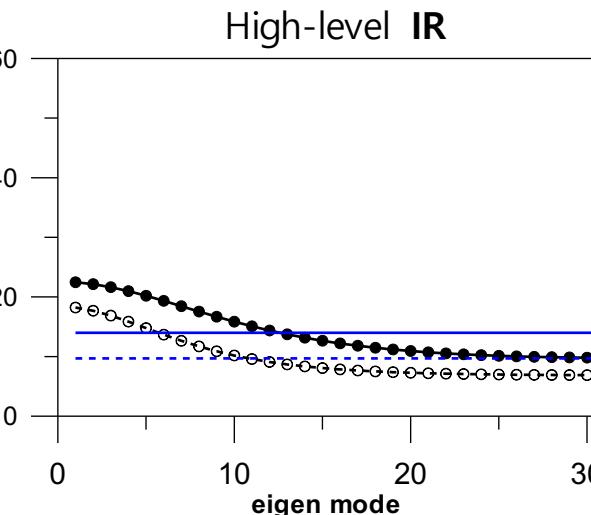
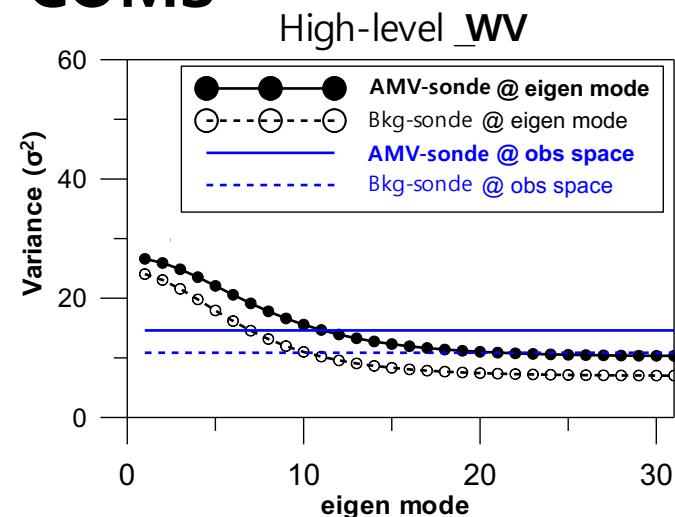
Error variance concentrated on governing eigen-mode is attributed to longer length scale of error correlation of MTSAT AMV.

On the other hand, relatively background error does not much intrude to large-scale pattern with its smaller correlation radius.

Compared to observation space, the variance ratio of AMV-sonde differences and bkg-sonde differences is amplified when the spatial error correlation error is reflected in eigen mode.

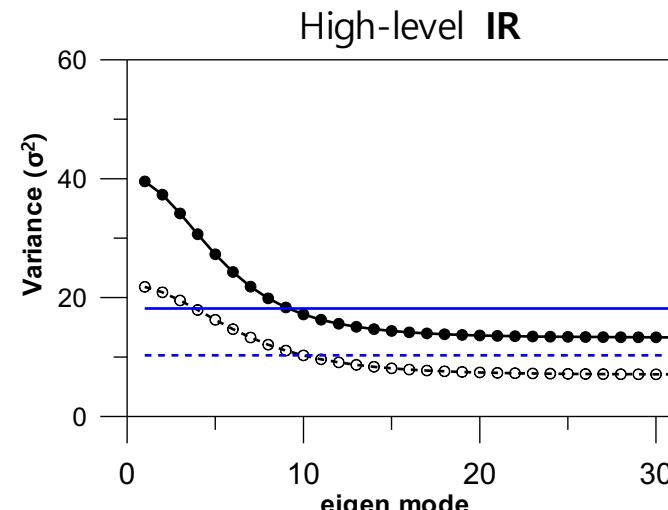
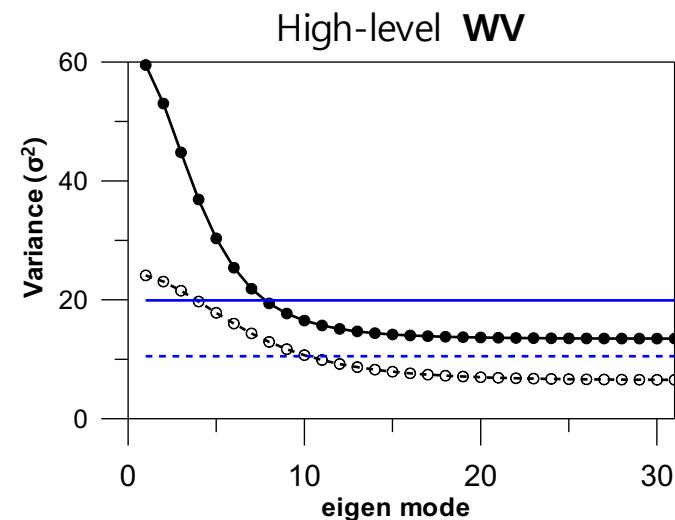
# Spatial Error Correlation

**COMS**



In high-level, the variance of the AMV-sonde differences is larger than that of background-sonde differences.

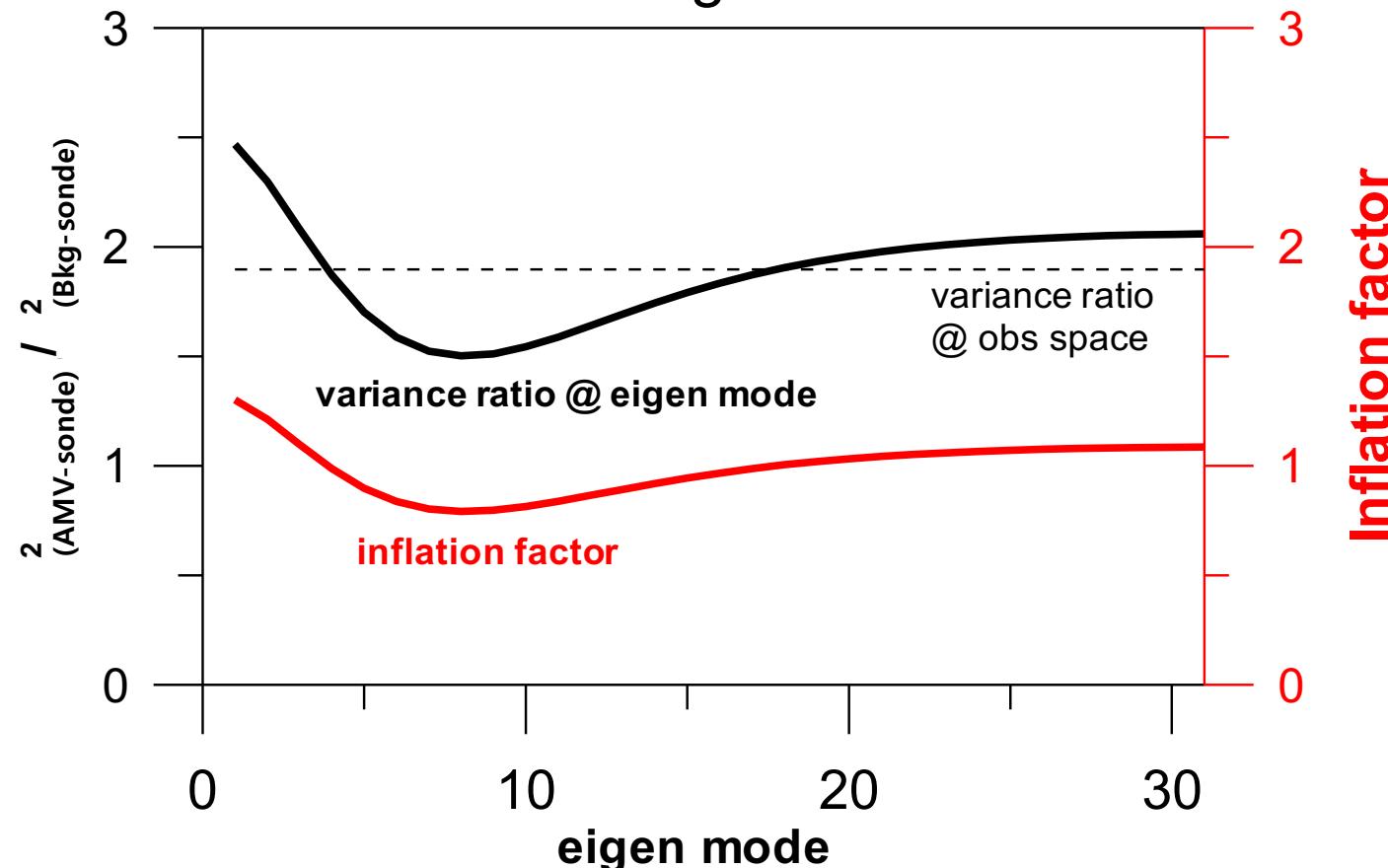
**MTSAT**



Especially, the variance ratio of spatially correlated MTSAT AMVs to background winds is 3 times larger in the governing eigen mode, compared to observation space with considering spatial error correlation.

# Inflation Factor

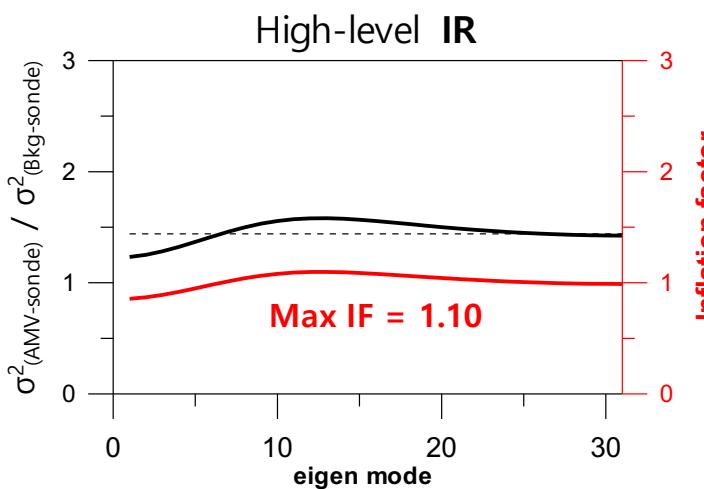
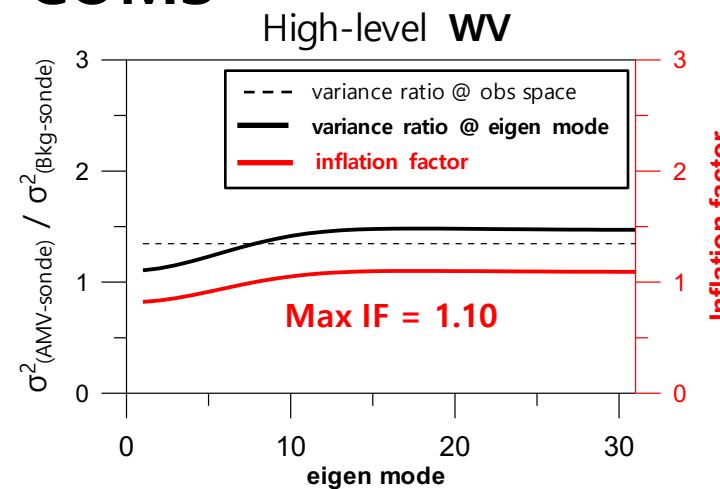
## MTSAT: High-level WV



The spatial correlations of the AMV errors account for inflation of observation error variation:  
Inflation factor = variance ratio @ eigen mode / variance ratio @ obs space

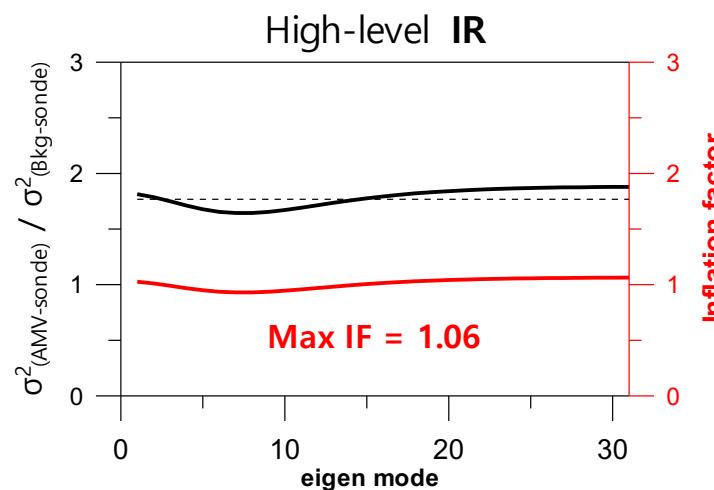
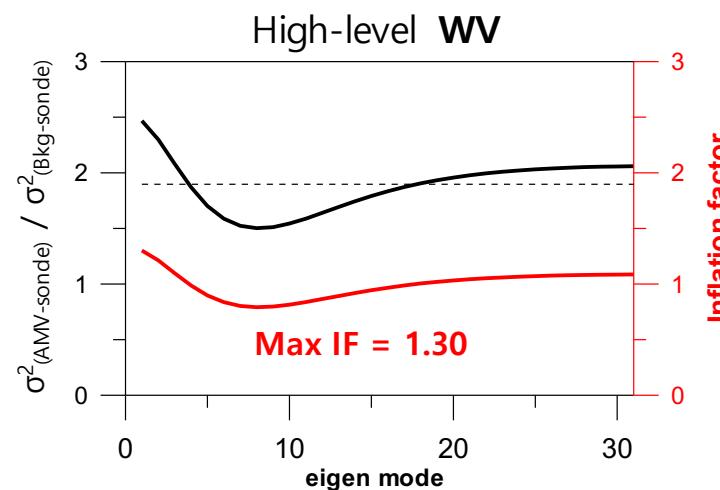
# Inflation Factor

## COMS



To consider spatial error correlations, observation error of high-level AMVs should be inflated about 1.10 ~ 1.30 times.

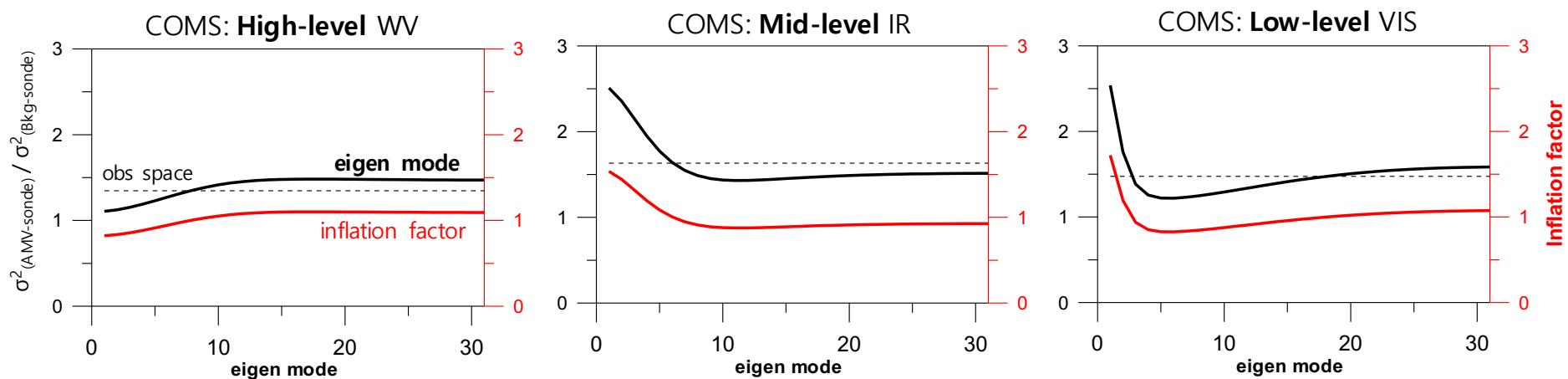
## MTSAT



MTSAT AMVs show the maximum inflation factor in the governing mode, but maximum inflation factor of COMS AMVs shows smaller eigen mode.

# COMS AMVs: Inflation Factor

COMS AMVs	Sample #	$L_{AMV}$	$L_{Bkg}$	Maximum inflation factor
High-level WV	34,128	0.90	1.09	1.10
Mid-level IR	56,639	1.71	0.89	1.54
Low-level VIS	17,978	6.33	0.56	1.72



In the **low-level**, the inflation factor of COMS AMVs from spatial error correlation is the highest up to 1.72. It is associated to larger length scale (of 6.33 degree) involving a dramatic integration of error variance on governing mode

- ❖ The ratio of AMV-sonde difference and background-sonde difference variances is amplified in eigen mode space where considering the spatial error correlation error.
- ❖ COMS and MTSAT AMVs show statistically significant spatial error correlations. In high-level, the correlation length scales of MTSAT AMVs are longer than those of COMS AMVs. It reflects advantage of COMS in retrieval algorithm, and so on...
- ❖ Spatial error correlations motivate to inflate observation error variance of MTSAT high-level-WV channel 1.3 times, while high-level COMS WV 1.1 times.
- ❖ Along vertical levels of COMS AMV, the inflation factor increases up to 1.72 responding to longer correlation length scale, 6.33 degree.

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**:Beyond the limit of the modern science and technology**

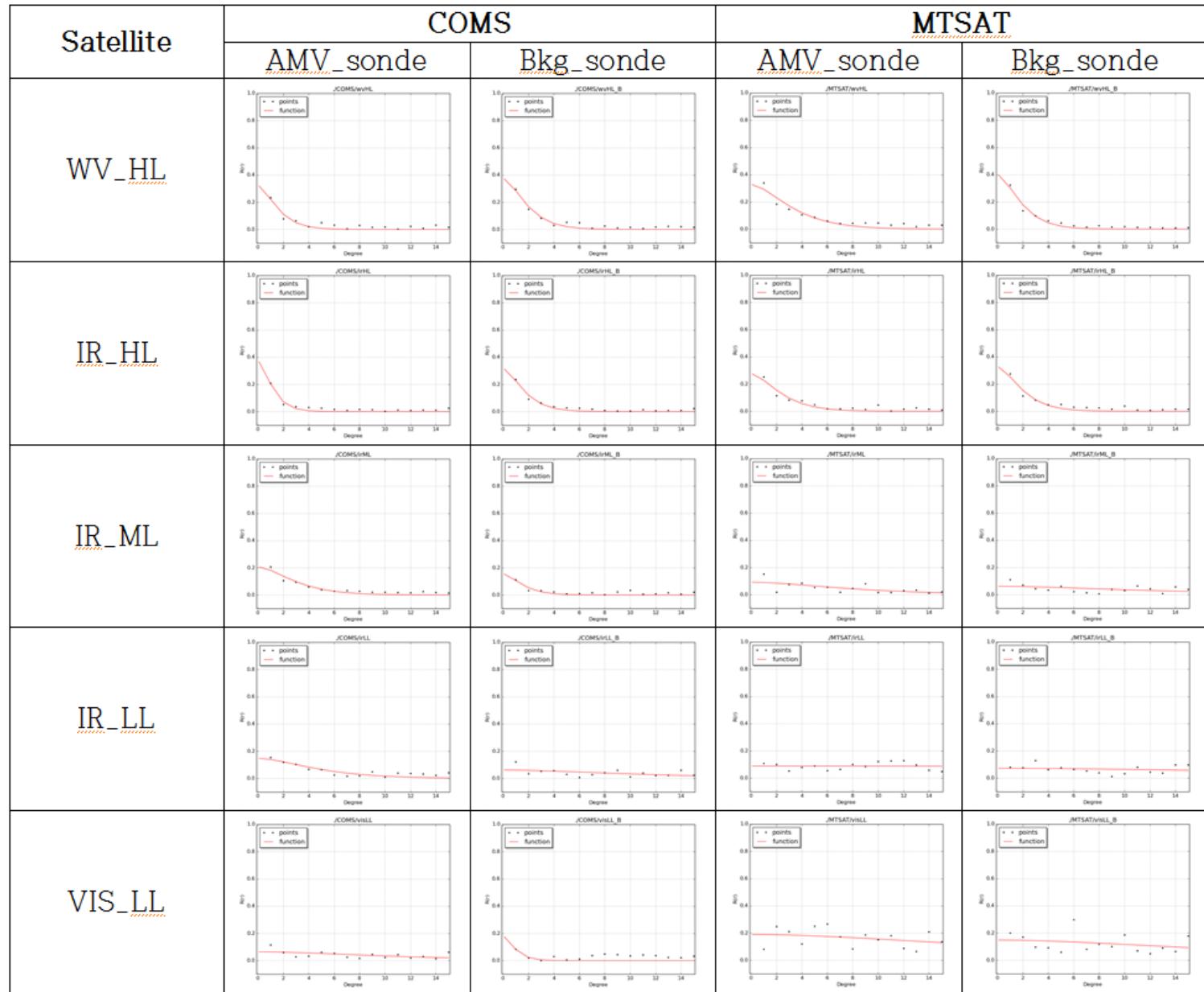
# Thank you



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# Back-up



## ❖ Fitting parameters of correlation function

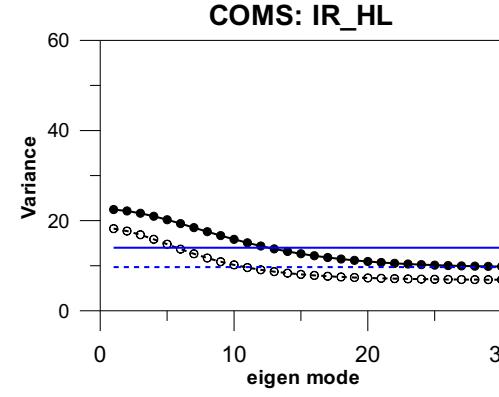
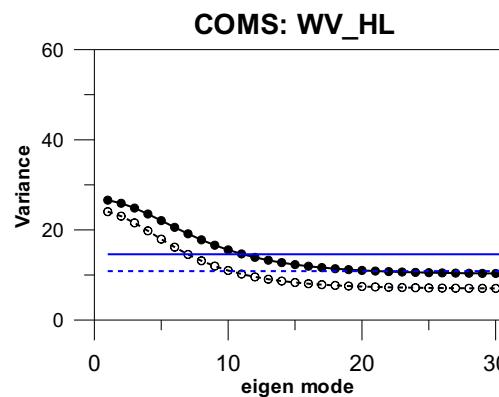
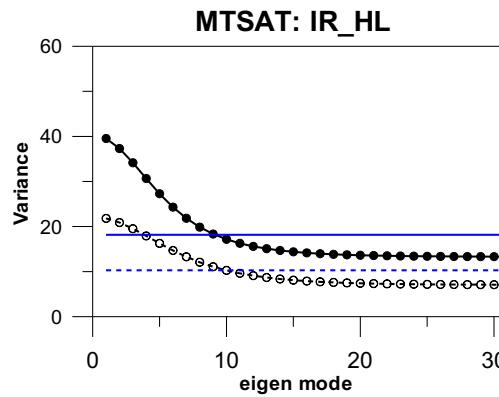
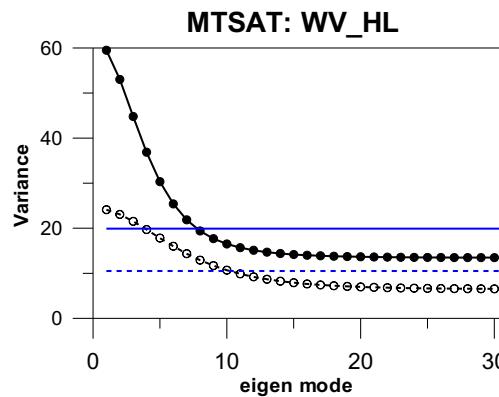
(1) AMV\_Sonde

Satellite	COMS		MTSAT	
	R0	L	R0	L
WV_HL	0.32	0.90	0.33	1.86
IR_HL	0.37	0.66	0.28	1.36
IR_ML	0.21	1.71	-	-
IR_LL	0.15	2.69	-	-
VIS_LL	0.06	6.33	-	-

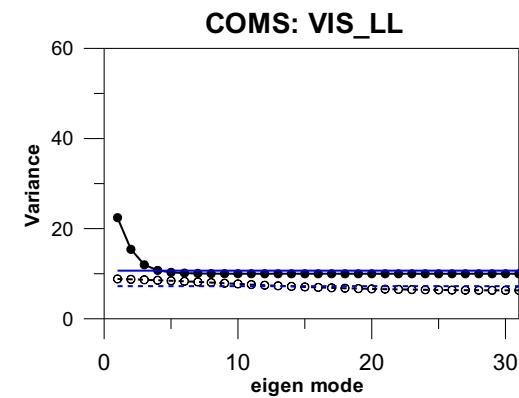
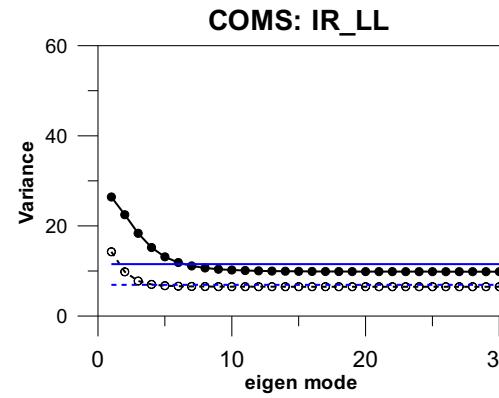
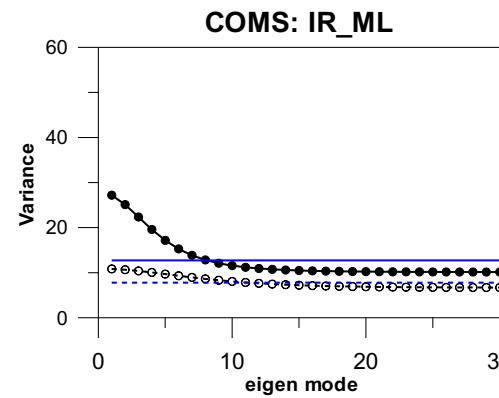
(2) Background\_Sonde

Satellite	COMS		MTSAT	
	R0	L	R0	L
WV_HL	0.37	1.09	0.40	1.08
IR_HL	0.32	0.96	0.33	1.13
IR_ML	0.15	0.89	-	-
IR_LL	0.06	6.43	-	-
VIS_LL	0.18	0.56	-	-

# Back-up



● Sonde\_AMV @ eigen mode  
○ Sonde\_Bkg @ eigen mode  
— Sonde\_AMV @ obs space  
- - - Sonde\_Bkg @ obs space



# Back-up

